Complex Adams invariants of sphere bundles associated to complex vector bundles over U-framed quasitoric manifolds

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In 1974, L. Smith gave a formula for the real Adams invariant of a reframed sphere bundle associated to a stably trivial real m-plane bundle over n-sphere, where m+n=4k.

In the talk we give a formula for the complex Adams invariant of a reframed sphere bundle associated to a complex vector bundle of rank q over any U-framed closed 2n-manifold M, and show that $q \leq 2$ holds.

If M is a quasitoric manifold over a simple polytope P, then the existence of a U-framing on M turns out to be equivalent to the n-colorability of P.

The talk is based on the ongoing project with Ivan Limonchenko.