The Stiefel-Whitney classes of a moment-angle manifold are trivial

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If a moment-angle complex Z_K is a smooth manifold, we can easily see that Z_K is null-cobordant (i.e. $Z_K = \partial M$ for some manifold with boundary M) and therefore the Stiefel–Whitney numbers of Z_K are trivial. This observation naturally leads us to ask the question: Are the Stiefel–Whitney classes of a moment-angle manifold also trivial? In this talk, I'd like to show that this problem can be solved affirmatively. Note that, by introducing the notion of Stiefel–Whitney classes for topological manifolds due to Fadell, we can consider this problem for the moment-angle manifolds which are topological manifolds, not only for smooth ones. For such cases, the problem is also solved affirmatively. Moreover, we also consider the Stiefel-Whitney classes of a partial quotient of a moment-angle manifold.